

Quiz 4

Name: _____

Solutions given without showing work will earn a zero. This quiz is closed-book. Circle your answers.

Problem 1. [6 points] Completely simplify the complex fraction

$$\begin{aligned}
 & \frac{\frac{x^2-1}{x^2-1}}{4 - \frac{1}{x^2-1}} \cdot \frac{4 + \frac{4}{x+1} + \frac{1}{x^2-1}}{4 + \frac{4}{x+1} + \frac{1}{x^2-1}} \\
 & \quad \text{Handwritten notes: } x^2-1 = (x+1)(x-1) \\
 & \quad \text{LCD} = (x+1)(x-1) = x^2-1 \\
 & = \frac{4(x^2-1) - \frac{1}{x^2-1} \cdot \frac{x^2-1}{1}}{4(x^2-1) + \frac{4}{x+1} \cdot \frac{(x+1)(x-1)}{1} + \frac{1}{x^2-1} \cdot \frac{x^2-1}{1}} \\
 & = \frac{4(x^2-1) - 1}{4(x^2-1) + 4(x-1) + 1} = \frac{4x^2 - 4 - 1}{4x^2 - 4 + 4x - 4 + 1} = \boxed{\frac{4x^2 - 5}{4x^2 + 4x - 7}}
 \end{aligned}$$

Problem 2. [4 points] Divide and simplify

$$\begin{aligned}
 & \frac{50x^2y^2 + 35x^3y^3 - 40x^4}{5x^2y^3} \\
 & \quad \text{Handwritten work: } \frac{50x^2y^2}{5x^2y^3} + \frac{35x^3y^3}{5x^2y^3} - \frac{40x^4}{5x^2y^3} \\
 & = \boxed{\frac{10}{y} + 7x - \frac{8x^2}{y^3}}
 \end{aligned}$$