

1. Odd Even Functions.

A function is said to be even if $f(-x) = f(x)$

A function is said to be odd if $f(-x) = -f(x)$

Determine if the given function is odd, even or neither.

a.
$$f(x) = \frac{1}{x^2 + 1}$$

b.
$$g(x) = x^5 - 3x^3$$

c.
$$h(x) = \frac{x}{x^3 - 1}$$

d.
$$f(x) = \frac{x}{x^2 + 1}$$

2. Symmetry

The graph of an even function is symmetric about the y-axis.

The graph of an odd function is symmetric about the origin.

Determine whether the given function is symmetric about the y axis, the origin or neither.

a.
$$f(x) = \frac{1}{x^2 + 1}$$

b.
$$f(x) = \frac{x}{x^2 + 1}$$

c.
$$h(x) = \frac{x}{x^3 - 1}$$

3. **Zeros**

The solutions to the equation $f(x) = 0$ are called the zeros of f .

Find all zeros of the given function.

a. $f(x) = x^2 - 7x - 10$

b. $g(x) = \frac{x^2 - 4x}{x^2 + 1}$

c. $h(x) = 1 + \sqrt{x - 2}$

4. **Intervals of Increase and Intervals of Decrease.**

A function is said to be increasing on an interval I if for all x in I , whenever $b > a$, we get $f(b) > f(a)$.

A function is said to be decreasing on an interval I if for all x in I , whenever $b > a$, we get $f(a) > f(b)$.

Find all intervals of increase and intervals of decrease of the given functions

a. $f(x) = x^2 - 4x + 1$

b. $g(x) = x^3 - x^2$ [G. Utility]

5. **Relative Extreme Values**

A function is said to have a minimum value at $x = a$ if the value of $f(a)$ is less than or equal to every value of f in a neighborhood of $x = a$.

Find all relative minimum values and all relative maximum values of the give functions

a. $f(x) = 2(x - 3)^2 + 4$

b. $g(x) = x^3 - x^2$ [G. Utility]