

Simplify each expression.

$$1. \frac{\sec(x) \sin(x)}{\tan(x) + \cot(x)}$$

$$2. \frac{\sec(x)}{\cos(x)} - \frac{\tan(x)}{\cot(x)}$$

$$3. \csc^2 x \tan^2 x - 1$$

$$4. (\sin x + \cos x)^2 + (\sin x - \cos x)^2$$

$$5. (\sin x + \cos x)(\tan x + \cot x)$$

$$6. \frac{\sin(x) + \tan(x)}{1 + \sec(x)}$$